

N.B. : (1) Question No. 1 is **compulsory**.

(2) Attempt any **four** questions from the remaining **five** questions.

1. (a) Derive the relationship between 2 transform, DTFT and DFT. 5
- (b) Find the step response of a system having difference equation. 5

$$y(n) = x(n) - 0.4 y(n - 1) + 0.05 y(n - 2)$$
- (c) Show that if $x(n]$ is odd signal then $\sum_{n=-\infty}^{\infty} x(n) = 0$ 5
- (d) Determine whether following signals are periodic 5
 (i) $\cos(0.3 \pi n + \pi/6)$ (ii) $x(n) = \sin(0.01 \pi n)$
2. (a) Using DIF-FFT find DFT of the following sequence 10
 $x(n) = \{1, 3, -2, 4, 1, 4, -2, 3\}$
- (b) Find the z transform of the following sequence and specify the ROC : 10
 (i) $x(n) = n \left(\frac{1}{4}\right)^n u(n)$ (ii) $x(n) = n u(-n - 1)$
3. (a) Find initial and final value of $x(n)$ for following causal system : 5
 (i) $x(z) = \frac{2z^2 + 1}{z^2 - 0.5z - 0.5}$ (ii) $x(z) = \frac{z}{z^2 + z - 1}$
- (b) Sketch the pole-zero plot for the system with transfer function : 5

$$H(z) = \frac{z^6 - 2^6}{z^5 (z - 2)}$$
 it the system stable.
- (c) Find the convolution and correlation of two sequences $x_1(n)$ and $x_2(n)$ 10
 $x_1(n) = [2, 1, 3]$ $x_2(n) = [-2, -1, 1]$
4. (a) Design a digital Butterworth filter satisfying the following constraints using bilinear transformation 10
 transformation
 Assume $T = 1S$

$$0.9 \leq |H(e^{jw})| \leq 1 \quad 0 \leq w \leq \pi/2$$

$$|H(e^{jw})| \leq 0.2 \quad 3\pi/4 \leq w \leq \pi$$
- (b) What is discrete hilbert transform ? Why it is used. 5
- (c) What are the conditions to be satisfied by LTI system. 5

5. (a) A low pass filter has desired response as given below

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$$H_d(e^{j\omega}) = \begin{cases} e^{-j3\omega} & 0 \leq \omega \leq \pi/2 \\ 0 & \pi/2 \leq \omega \leq \pi \end{cases}$$

Determine the filter coefficient $h(n)$ for $M = 7$ using frequency sampling technique.

(b) Impulse response of LTI system is $h(n) = \{1 \underset{\uparrow}{2} -1 \ 3\}$

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Determine the output response of the system to input $x(n) = \{1 \underset{\uparrow}{2}, 3, 1\}$

6. Write short notes on :-

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- (a) Application of DSP in Telecommunication
 - (b) DSP processors
 - (c) Fetal ECG monitoring
 - (d) Chirp 2 Algorithm.
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