

Sem-III ETRX, CBS GS 23/11/17  
**Q.P. Code: 10592**

[Time: 3 Hours]

Please check whether you have got the right question paper.

**N.B:**

1. **Question -1 is compulsory.**
2. **Solve any THREE from remaining questions.**
3. Assume suitable data if necessary.

- 1 a) Explain two terminal Mos structure. (05)
- b) Calculate width of the space charge region in a PN junction when a reverse bias voltage is applied consider a P-N junction at  $T = 300 \text{ K}$ ,  $N_A = 10^{16} \text{ cm}^{-3}$  and  $N_D = 10^{15} \text{ cm}^{-3}$ ,  $n_t = 1.5 \times 10^{10} \text{ cm}^{-3}$  and  $V_R = -5 \text{ V}$ ,  $V_{bi} = 0.635 \text{ V}$ .  $V_{bi}$  is the built in potential barrier voltage. (05)
- c) Write note on HBT. (05)
- d) Explain differences between FET and MESFET. (05)
- 2 a) Explain construction working and characteristics of Tunnel diode. (10)
- b) Draw and explain hybrid  $\pi$  (pi) model of BJT. (10)
- 3 a) Calculate  $V_{bi}$  in a silicon P-N junction at  $T = 300 \text{ K}$  for  $N_D = 10^{15} \text{ cm}^{-3}$  and  $N_A = 10^{14} \text{ cm}^{-3}$  and  $n_i = 1.5 \times 10^{10} \text{ cm}^{-3}$ . (10)
- b) Explain constructions working and characteristics of J-E MOSFET. (10)
- 4 a) Explain construction, working and characteristics of FET. (10)
- b) Explain following effects in FET - (1) Channel length modulation (2) Velocity saturation effects. (10)
- 5 a) Draw and explain energy band diagram for MOSFET for different gate bias conditions. (10)
- b) Explain working and characteristics of SCR. (10)
- 6 Write notes on any four of the following (20)
  - a) Zener diode voltage regulator
  - b) Triac
  - c) Solar Cell
  - d) Photo diode
  - e) UJT relaxation oscillator

Applied Mathematics - III

29/11/17

( 3 Hours)

I. Total marks : 80

Note :-

- 1) Question number 1 is compulsory.
- 2) Attempt any three questions from the remaining five questions.
- 3) Figures to the right indicate full marks.

Q.1 a) Find the angle between the surfaces

$$x \log z + 1 - y^2 = 0, \quad x^2y + z = 2 \text{ at } (1, 1, 1).$$

b) Show that the functions  $f_1(x) = 1$ ,  $f_2(x) = x$  are orthogonal on

$(-1, 1)$ . Determine the constants  $a$  and  $b$  such that the function

$f_3(x) = -1 + ax + bx^2$  is orthogonal to both  $f_1$  and  $f_2$  on that interval.

c) Find the Laplace transform of  $\int_0^t u^{-1} e^{-u} \sin u \, du$ .

d) Prove that  $f(z) = (x^3 - 3xy^2 + 2xy) + i(3x^2y - x^2 + y^2)$  is analytic and find  $f'(z)$  and  $f(z)$  in terms of  $z$ .

Q.2 a) Obtain half-range sine series of  $f(x) = x(\pi - x)$  in  $(0, \pi)$  and hence, find the value of  $\sum_{n=1}^{\infty} \frac{(-1)^n}{(2n-1)^3}$ .

b) Prove that

$\bar{F} = (y^2 \cos x + z^3) i + (2y \sin x - 4) j + (3xz^2 + 2) k$

is a conservative field. Find the scalar potential for  $\bar{F}$ .

c) Find the inverse Laplace transform of

$$\frac{s+2}{s^2 - 4s + 13}$$

$$\frac{1}{(s-a)(s-b)}$$

Prove that  $\int_{-\infty}^{\infty} x^2 e^{-xt} dx = \sqrt{\frac{\pi}{x}} \left( \frac{3-x^2}{x^2} \sin x - \frac{3}{x} \cos x \right)$ .

b) Find the analytic function  $f(z) = u + iv$  if

$$3u + 2v = x^2 + 16xy.$$

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- c) Expand  $f(x) = \begin{cases} \pi x, & 0 < x < 1 \\ 0, & 1 < x < 2 \end{cases}$  period 2 into a Fourier Series.

Q. 4 a) Prove that

$$\int x^3 \cdot J_0(x) dx = x^3 \cdot J_1(x) - 2x^2 \cdot J_2(x)$$

- b) Use Stoke's Theorem to evaluate  $\int_C \bar{F} \cdot d\bar{r}$   
where  $\bar{F} = yz i + zx j + xy k$   
and  $C$  is the boundary of the circle  $x^2 + y^2 = 1$ .

- c) Solve using Laplace transform  $(D^2 + 3D + 2)y = 4e^{-2t}$  with  
 $y(0) = -3$  and  $y'(0) = 5$ .

Q. 5 a) Prove that  $2J_0''(x) = J_2(x) - J_0(x)$

- b) Use Laplace transform to evaluate

$$\int_0^\infty e^{-t} \left( \int_0^t u^2 \sin hu \cos hu du \right) dt$$

- c) Obtain complex form of Fourier Series for  $f(x) = e^{ax}$  in  $(-\pi, \pi)$   
where  $a$  is not an integer. Hence deduce that when  $a$  is a constant other than an integer

$$\cos ax = \frac{\sin \pi a}{\pi} \sum_{n=0}^{\infty} \frac{(-1)^n a^n}{(\alpha^2 - n^2)} e^{inx}$$

Q. 6 a) Express the function

$$f(x) = \begin{cases} -e^{kx} & \text{for } x < 0 \\ e^{-kx} & \text{for } x > 0 \end{cases}$$

as Fourier Integral and hence, prove that

$$\int_{-\infty}^{\infty} \frac{\omega \sin \omega x}{\omega^2 + k^2} d\omega = \frac{\pi}{2} e^{-kx} \quad \text{if } x > 0, k > 0.$$

b) Using Green's theorem evaluate

$$\oint_C (e^{x^2} - xy) dx - (y^2 - ax) dy$$

where  $C$  is the circle  $x^2 + y^2 = a^2$ .

- c) Under the transformation  $w = \frac{z-1}{z+1}$ , show that the map of the straight line  $y=x$  is a circle and find its center and radius.

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